



# Web Structure & Content

(not a theory talk)

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Research supported by NSF  
CAREER Award IIS-0133124



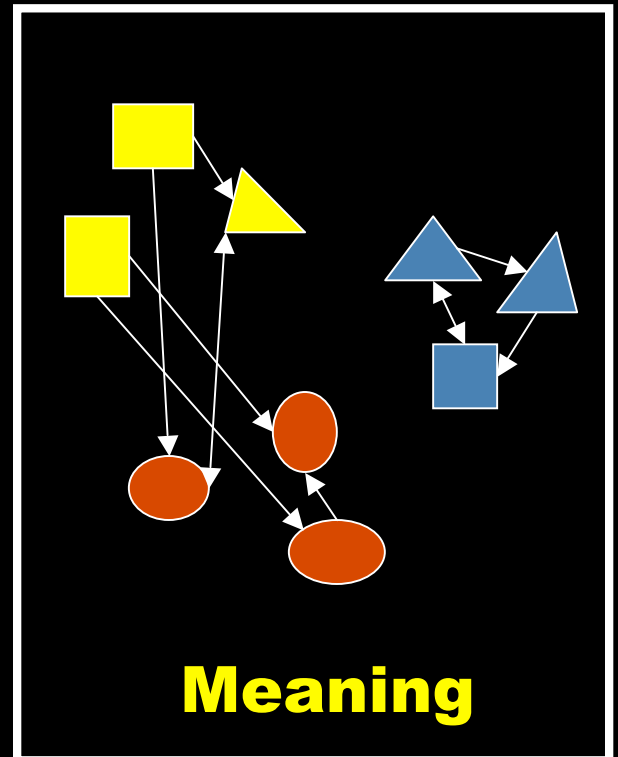
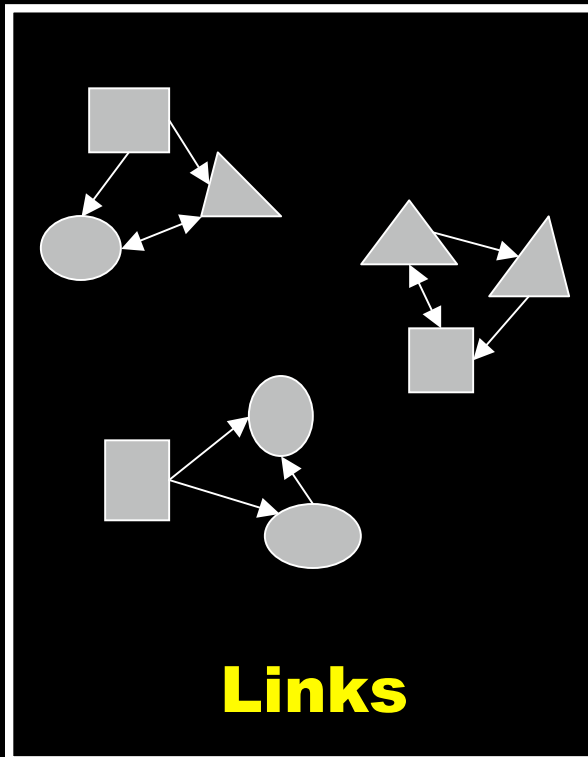
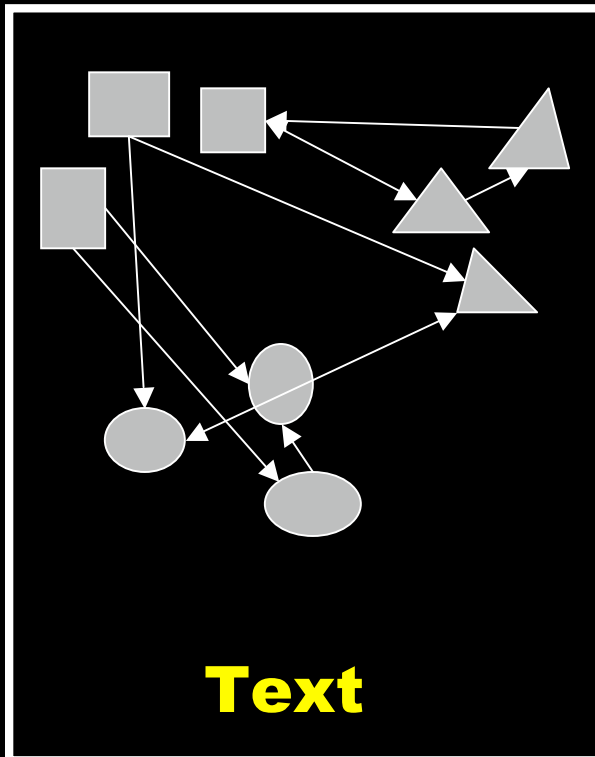
# Exploiting the Web's text and link cues

- *Pages close in word vector space tend to be related*
  - Cluster hypothesis (van Rijsbergen 1979)
  - The WebCrawler (Pinkerton 1994)
  - The whole first generation of search engines
- *Pages that link to each other tend to be related*
  - Link-cluster conjecture (Menczer 1997)
    - Many formulations: Gibson & al 1998, Bharat & Henzinger 1998, Chakrabarti & al 1998, Dean & Henzinger 1999, Davison 2000, etc
  - Link eigenvalue analysis: HITS, hubs and authorities
    - (Kleinberg & al 1998 segg. @ Almaden etc.)
  - Google's PageRank analysis
    - (Brin & Page 1998)
  - The whole second generation of search engines



# Three topologies

What about the *relationship* between  
**lexical** / **link** cues and page **meaning**?





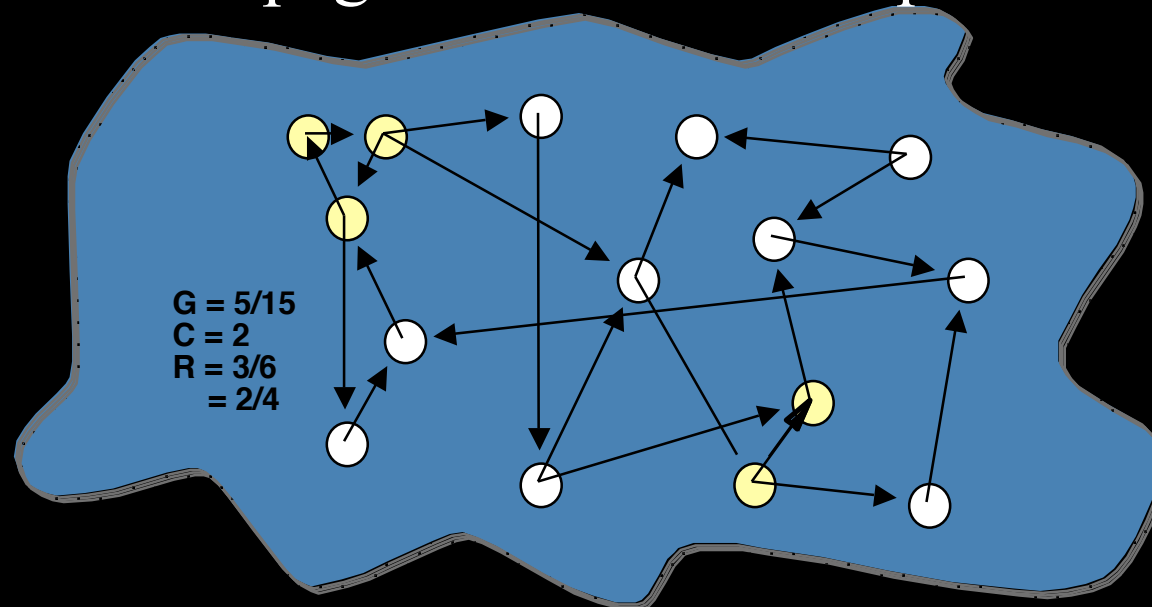
# Talk outline

- The topologies of the Web
- Correlations, distributions, projections
- Power laws and Web growth models
- Navigating optimal paths
- Semantic maps (?)



# The “link-cluster” conjecture

- Connection between **semantic** topology (relevance) and **linkage** topology (hypertext)
  - $G = \Pr[\text{rel}(p)] \sim$  fraction of relevant pages (generality)
  - $R = \Pr[\text{rel}(p) \mid \text{rel}(q) \text{ AND } \text{link}(q,p)]$
- Related nodes are clustered if  **$R > G$** 
  - Necessary and sufficient condition for a random crawler to find pages related to start points

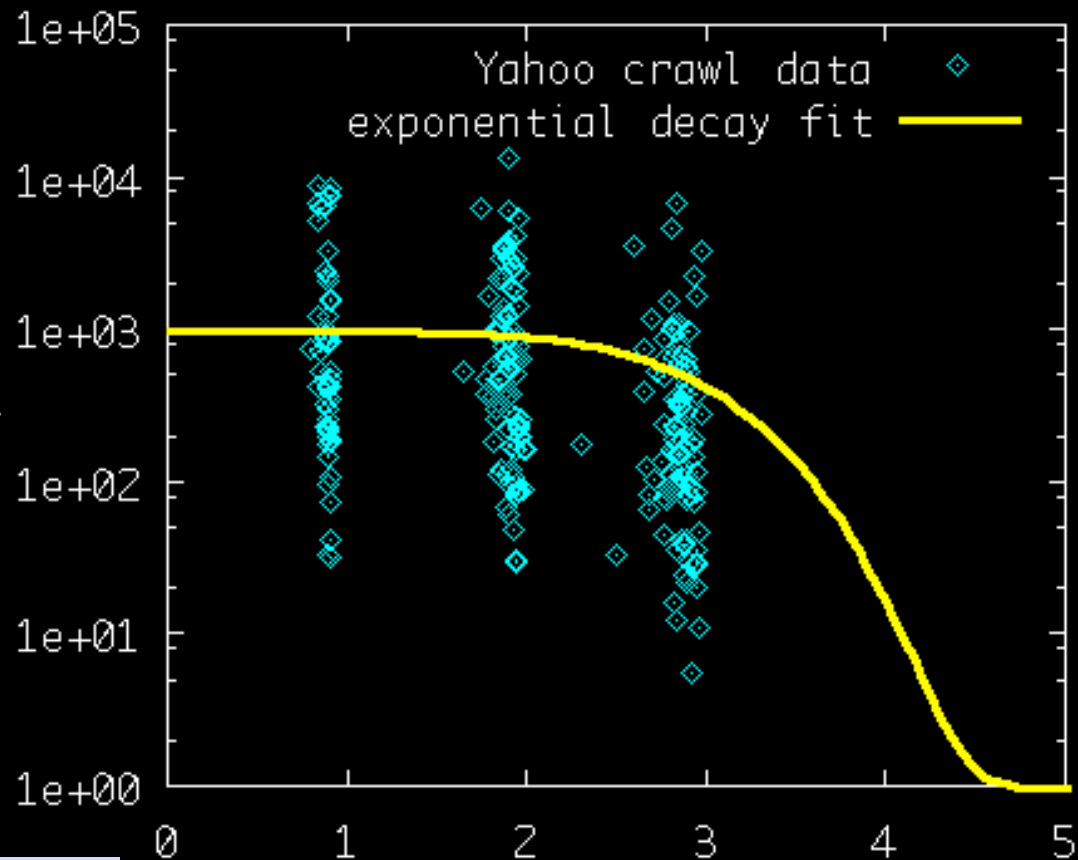




$$\frac{R(q, \square)}{G(q)} \equiv \frac{\Pr[rel(p) | rel(q) \square \| path(q, p) \| \square \square]}{\Pr[rel(p)]}$$

## Link-cluster conjecture

- Preservation of **semantics** (meaning) across **links**



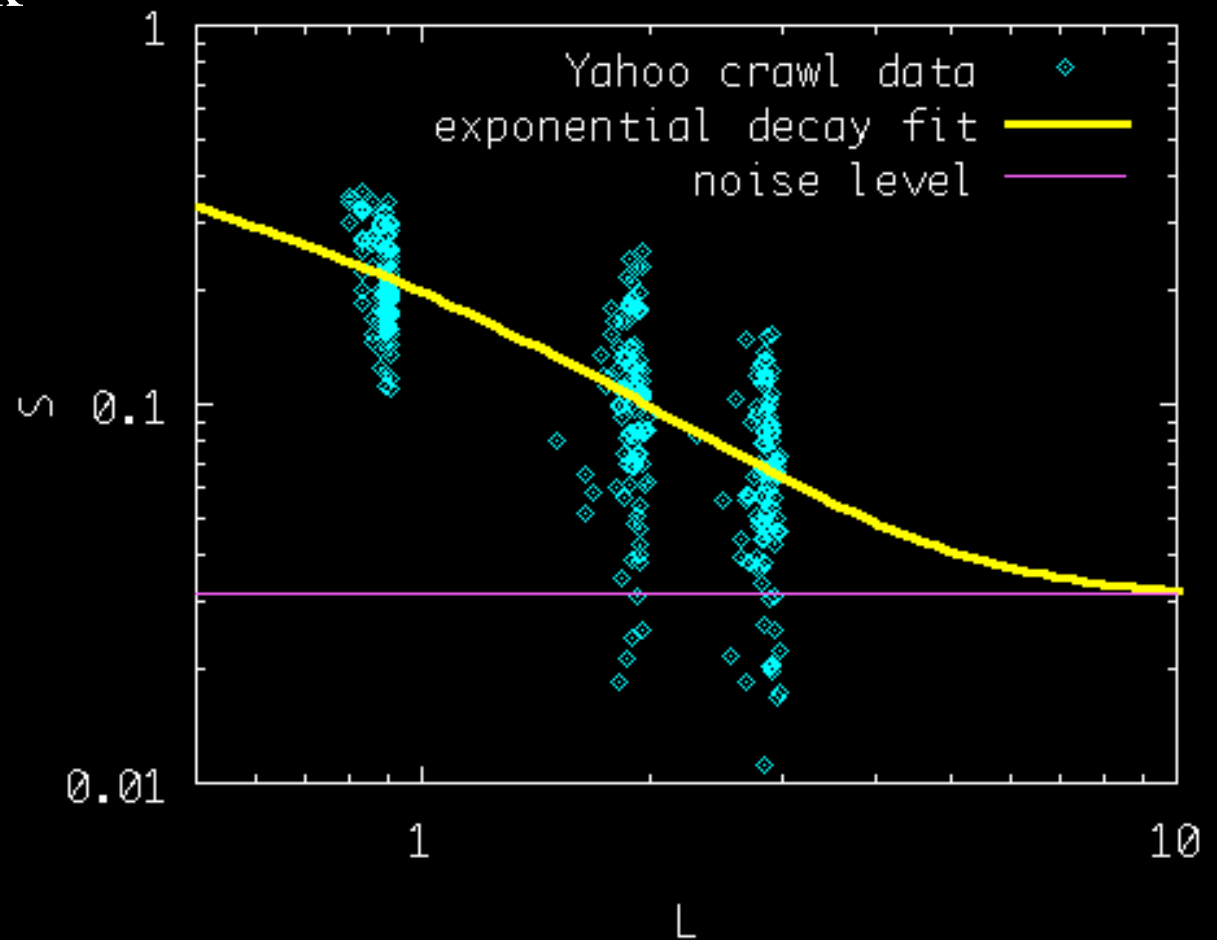
$$L(q, \square) \equiv \frac{\square \| path(q, p) \|}{|\{p : \| path(q, p) \| \square \square\}|}$$



# The “link-content” conjecture

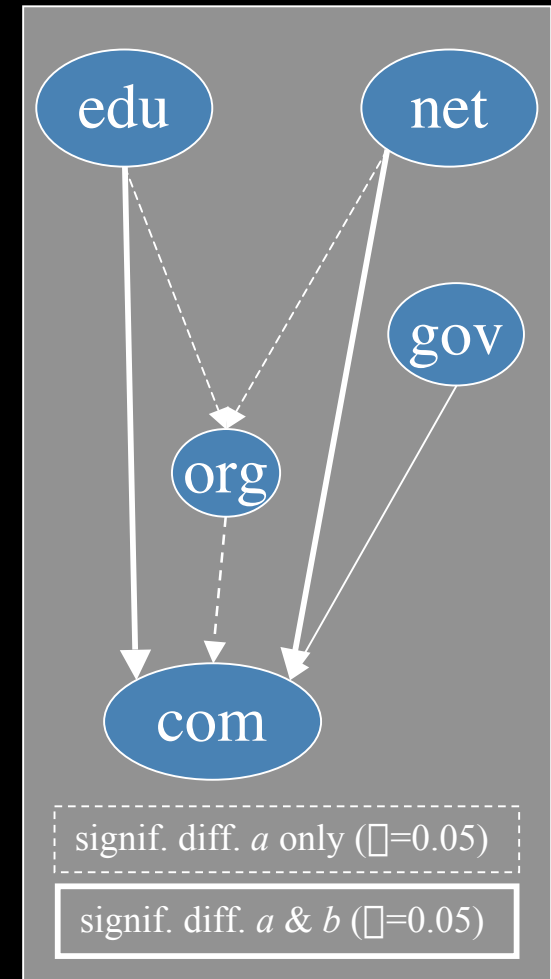
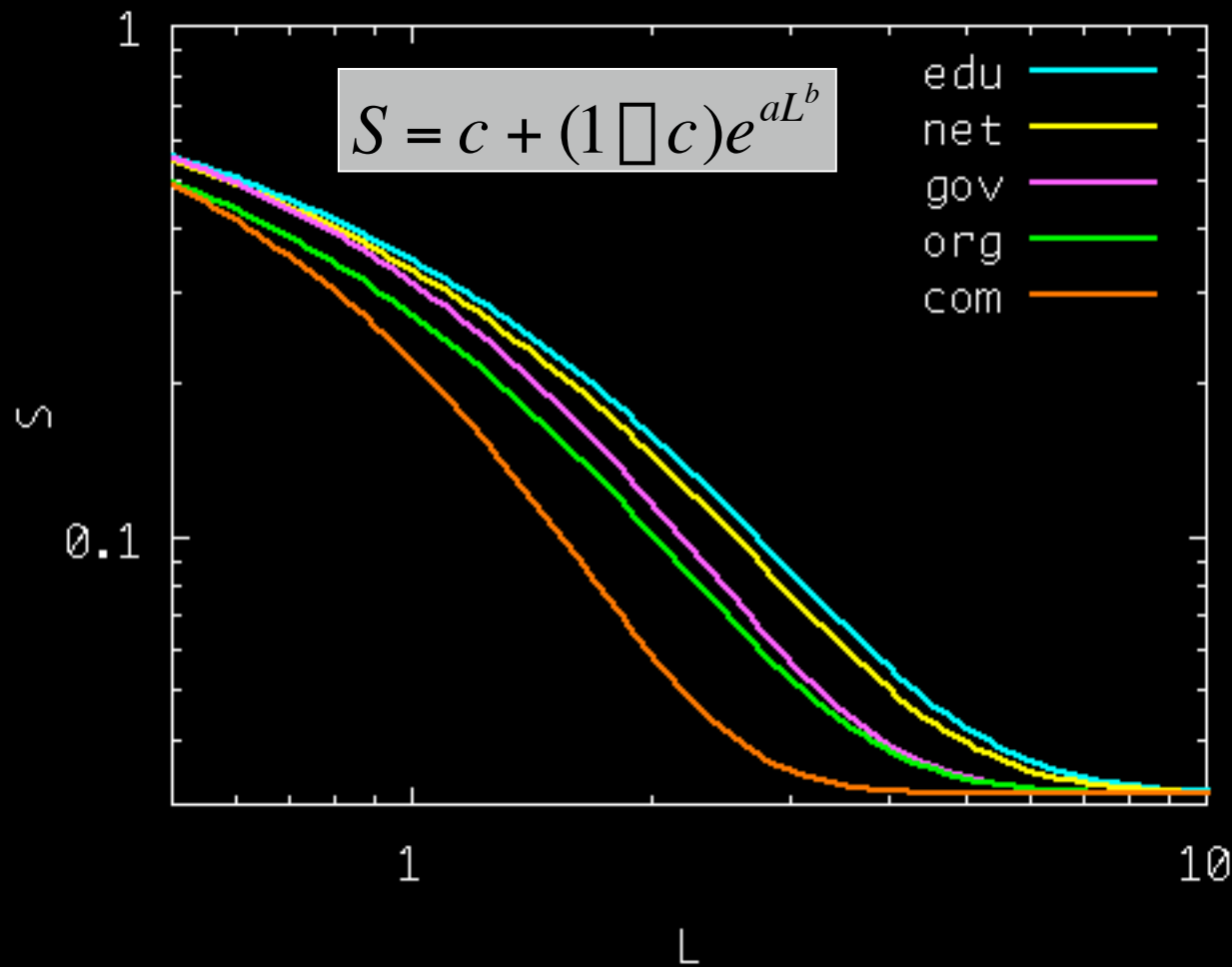
- Correlation of **lexical** and **linkage** topology
- $L(\square)$ : average link distance
- $S(\square)$ : average similarity to start (topic) page from pages up to distance  $\square$
- Correlation  $\rho(L, S) = -0.76$

$$S(q, \square) \equiv \frac{\sum_{p: \|path(q, p)\| \leq \square} sim(q, p)}{|\{p: \|path(q, p)\| \leq \square\}|}$$





# Heterogeneity of lexical-linkage correlation





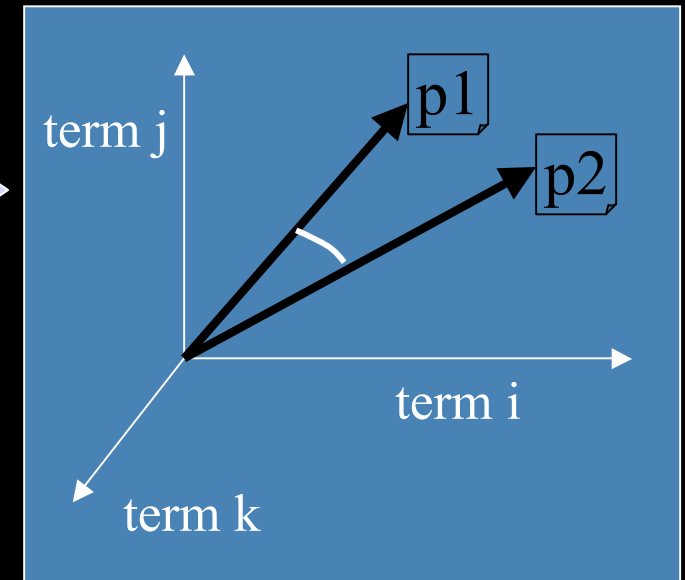


# Mapping the relationship between topologies

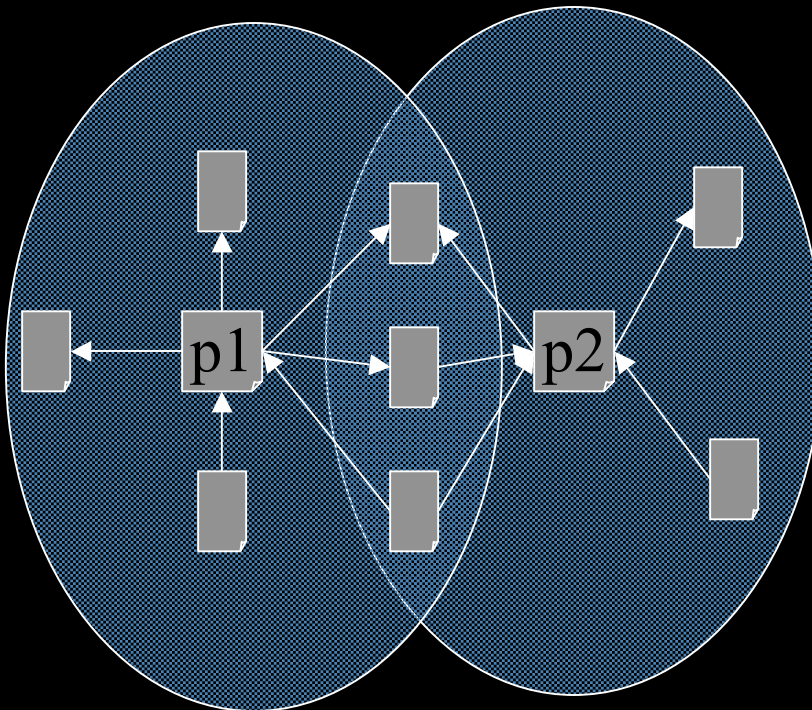
- Any pair of pages rather than linked pages from crawl
- Data: Open Directory Project ([dmoz.org](http://dmoz.org))
  - RDF Snapshot: 2002-02-14 04:01:50 GMT
  - After cleanup: 896,233 URLs in 97,614 topics
  - After sampling: 150,000 URLs in 47,174 topics
    - 10,000 from each of 15 top-level branches
- Need ‘similarity’ or ‘proximity’ metric for each topology, given a pair of pages:
  - **Content**: textual/lexical (cosine) similarity
  - **Link**: co-citation/bibliographic coupling
  - **Semantic**: relatedness inferred from manual classification



$$\cos_c(p_1, p_2) = \frac{\sum_{k \in p_1 \cap p_2} f_{kp_1} f_{kp_2}}{\sqrt{\sum_{k \in p_1} f_{kp_1}^2 \sum_{k \in p_2} f_{kp_2}^2}}$$



Content similarity



Link similarity

$$\cos_l(p_1, p_2) = \frac{|U_{p_1} \cap U_{p_2}|}{|U_{p_1} \cup U_{p_2}|}$$



# Semantic similarity

$$\square_s(c_1, c_2) = \frac{2\log\Pr[lca(c_1, c_2)]}{\log\Pr[c_1] + \log\Pr[c_2]}$$

- Information-theoretic measure based on classification tree (Lin 1998)
- Classic path distance in special case of balanced tree

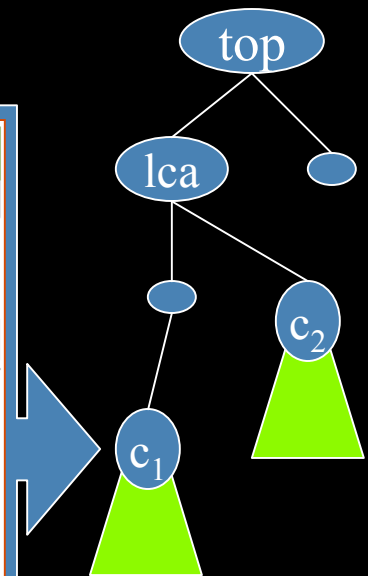
dmoz open directory project

about dmoz | add URL | update URL | become an editor | help

Search the entire kids and teens directory

**Kids and Teens: People and Society: Holidays and Celebrations: Birthdays (11)** [Description](#)

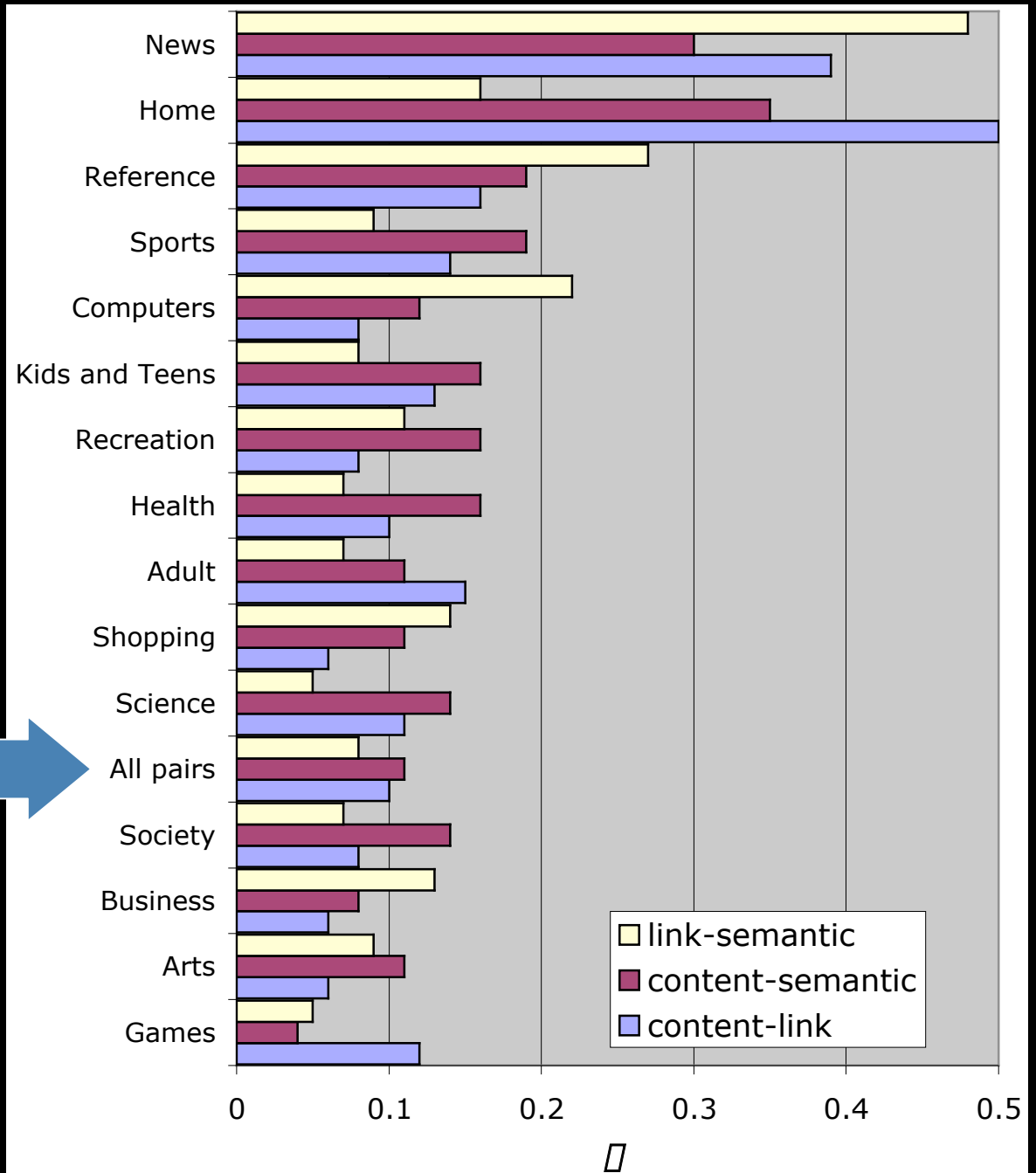
- [Billy Bear's Birthday Party](#) [ Kids ] – Offers printable projects, downloads, games, and an online cake baking contest.
- [Birthday Celebrations Net](#) [ Kids/Teens ] – Features songs, traditions and recipes from around the world.
- [Birthday Traditions From Around the World](#) [ Kids/Teens ] – Describes the origin of birthday celebrations and various family and cultural traditions.
- [Cyber Grandma's Birthday Party](#) [ Kids ] – Filled with online party games and songs.
- [DLTK's Birthday Crafts for Kids](#) [ Kids ] – Free printable craft templates designed for younger kids.
- [Fun Facts about Happy Birthday to You](#) [ Kids/Teens/Mature Teens ] – Discover the history of this well-known ditty.
- [Happy Birthday from PrimaryGames.com](#) [ Kids ] – Games, musical postcards, gift tags, and stationery.
- [Happy Birthday to You](#) [ Kids/Teens ] – Offers online games and puzzles, printable activities, coloring pages, free clip art, screen savers, animated greeting cards, and downloads.
- [Ivy's Birthday Greeting Cards to Print](#) [ Kids/Teens ] – Greeting cards to make, print, fold, and mail or give to friends.
- [Ways to Say Happy Birthday](#) [ Kids/Teens/Mature Teens ] – Learn over 150 ways to say Happy Birthday in different languages.
- [Webmonkey for Kids: Birthday Invitation](#) [ Kids/Teens ] – A step-by-step guide to creating an online party invitation.





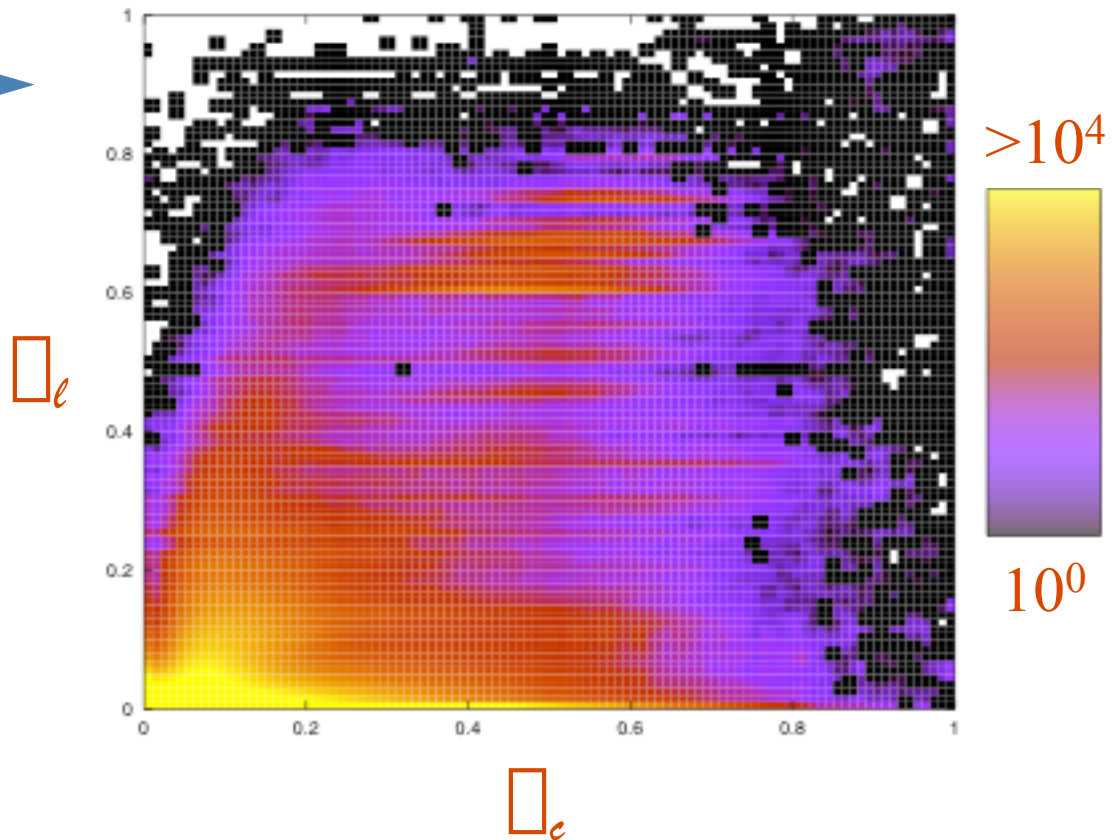
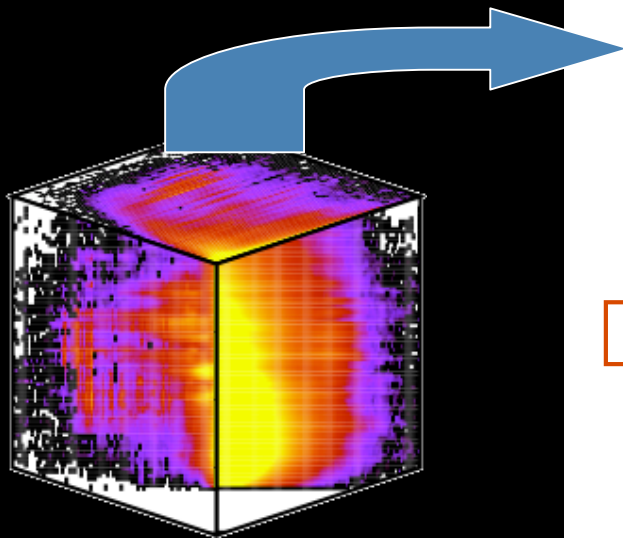
# Correlations between similarities

$3.84 \times 10^9$   
pairs





# Joint distribution cube

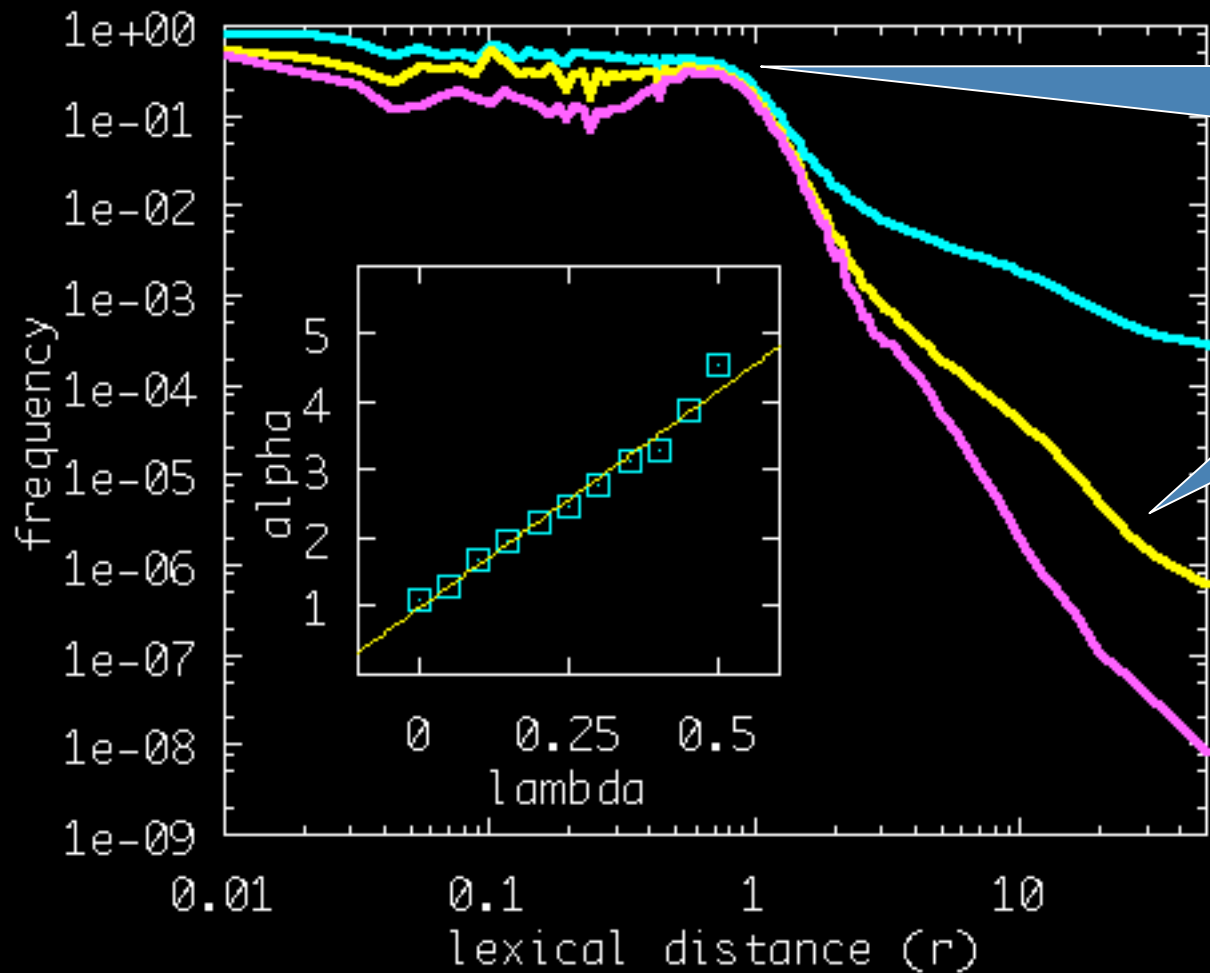




# Link probability vs lexical distance

$$r = \frac{1}{\Delta_c} \sum_i 1$$

$$\Pr(\Delta | \Delta) = \frac{|(p, q) : r = \Delta \Delta \Delta_i > \Delta|}{|(p, q) : r = \Delta|}$$



Phase  
transition

$\Delta^*$

Power law tail  
 $\Pr(\Delta | \Delta) \sim \Delta^{-\alpha(\Delta)}$

*Proc. Natl.  
Acad. Sci. USA*  
99(22): 14014-  
14019, 2002  
WAW 2002



# Web growth models

- Preferential attachment “BA”

- At each step  $t$  add page  $p_t$
- Create  $m$  new links from  $p_t$  to  $p_{i < t}$

(Barabasi & Albert 1999, de Solla Price 1976)

$$\Pr(i) \propto k(i)$$

- Modified BA

(Bianconi & Barabasi 2001, Adamic & Huberman 2000)

$$\Pr(i) \propto \alpha(i) k(i)$$

- Mixture

(Pennock & al. 2002,  
Cooper & Frieze 2001, Dorogovtsev & al 2000)

$$\Pr(i) \propto \alpha \cdot k(i) + (1 - \alpha) \cdot c$$

- Web copying

(Kleinberg, Kumar & al 1999, 2000)

$$\Pr(i) \propto \alpha \cdot \Pr(j \rightarrow i) + (1 - \alpha) \cdot c$$

- Mixture with Euclidean distance in graphs

(Fabrikant, Koutsoupias & Papadimitriou 2002)

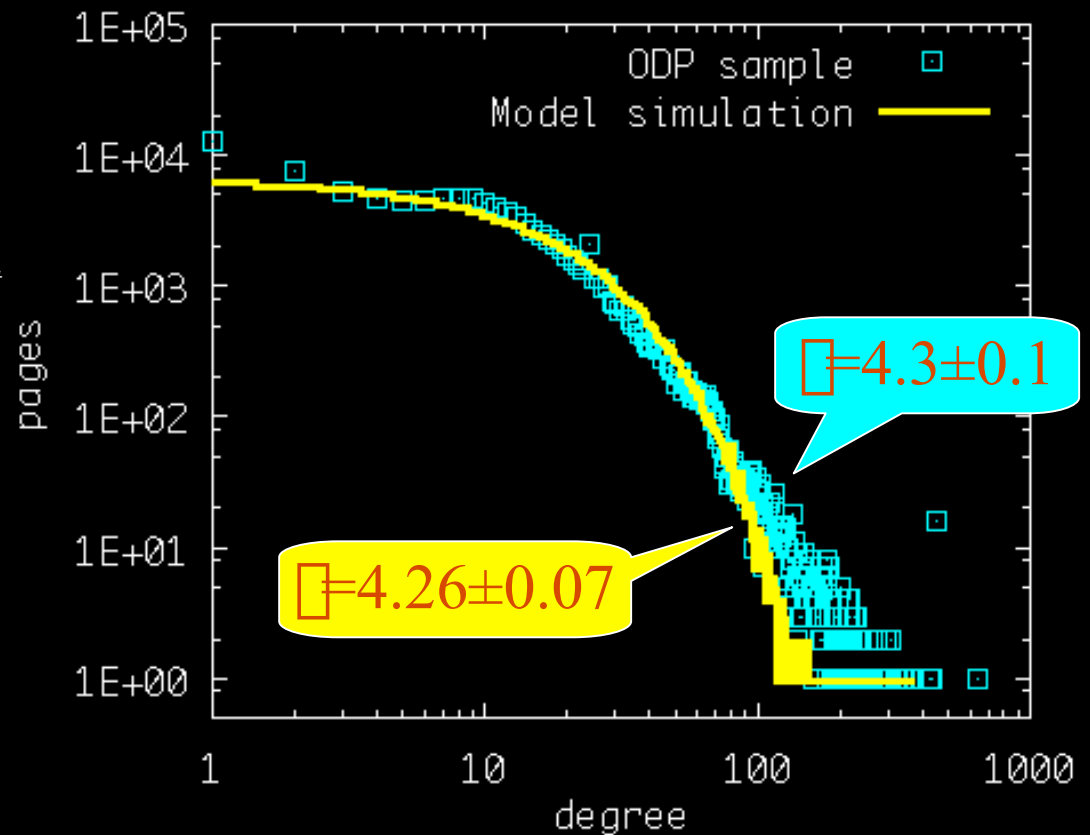
$$i = \arg \min (\alpha r_{it} + g_i)$$



# Local content-based growth model

$$\Pr(p_t \rightarrow p_{i < t}) = \begin{cases} \frac{k(i)}{mt} & \text{if } r(p_i, p_t) < \tau^* \\ c[r(p_i, p_t)]^\alpha & \text{otherwise} \end{cases}$$

- Similar to preferential attachment (BA)
- At each step  $t$  add page  $p_t$
- Create  $m$  new links from  $p_t$  to existing pages
- Use degree ( $k$ ) info only for nearby pages  
(popularity/importance of similar/related pages)







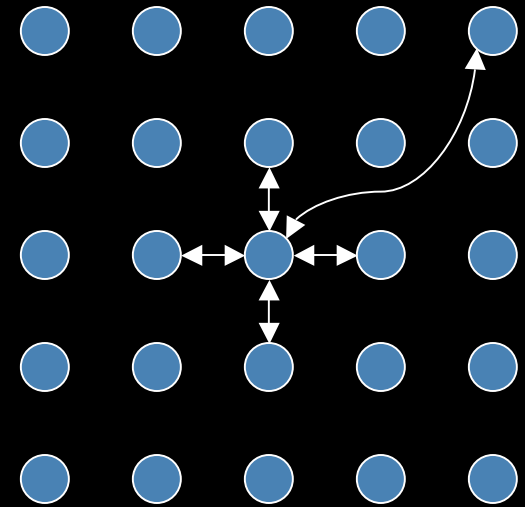
# Efficient crawling algorithms?

- Theory: since the Web is a small world network, or has a scale free degree distribution, **there exist short paths** between any two pages:
  - $\sim \log N$  (Barabasi & Albert 1999)
  - $\sim \log N / \log \log N$  (Bollobas 2001)
- Practice: **can't find them!**
  - Greedy algorithms based on location in geographical small world networks:  $\sim \text{poly}(N)$  (Kleinberg 2000)
  - Greedy algorithms based on degree in power law networks:  $\sim N$  (Adamic, Huberman *et al* 2001)



# Exception # 1

- Geographical networks (Kleinberg 2000)
  - Local links to all lattice neighbors
  - Long-range link probability distribution: power law  $\Pr \sim r^{-\beta}$ 
    - $r$ : lattice (Manhattan) distance
    - $\beta$ : constant clustering exponent

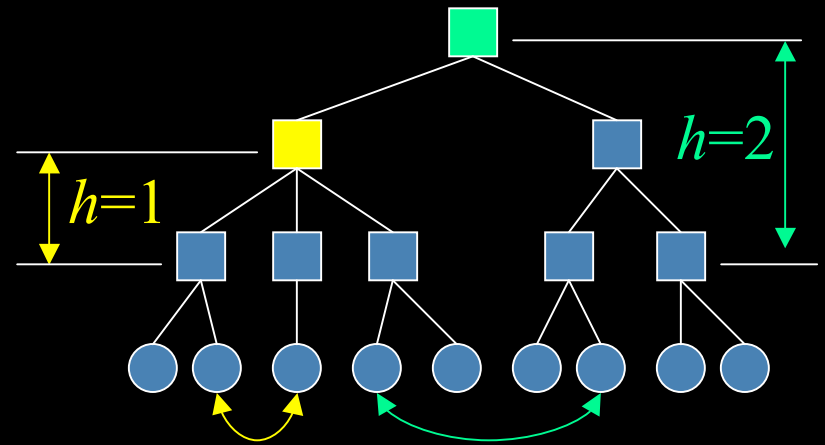


$$t \sim \log^2 N \quad \beta = D$$



## Exception # 2

- Hierarchical networks  
(Kleinberg 2002, Watts & *al.* 2002)
  - Nodes are classified at the leaves of tree
  - Link probability distribution: exponential tail  
 $\Pr \sim e^{-h}$ 
    - $h$ : tree distance (height of lowest common ancestor)



$$t \sim \log^{\square} N, \square \geq 1$$

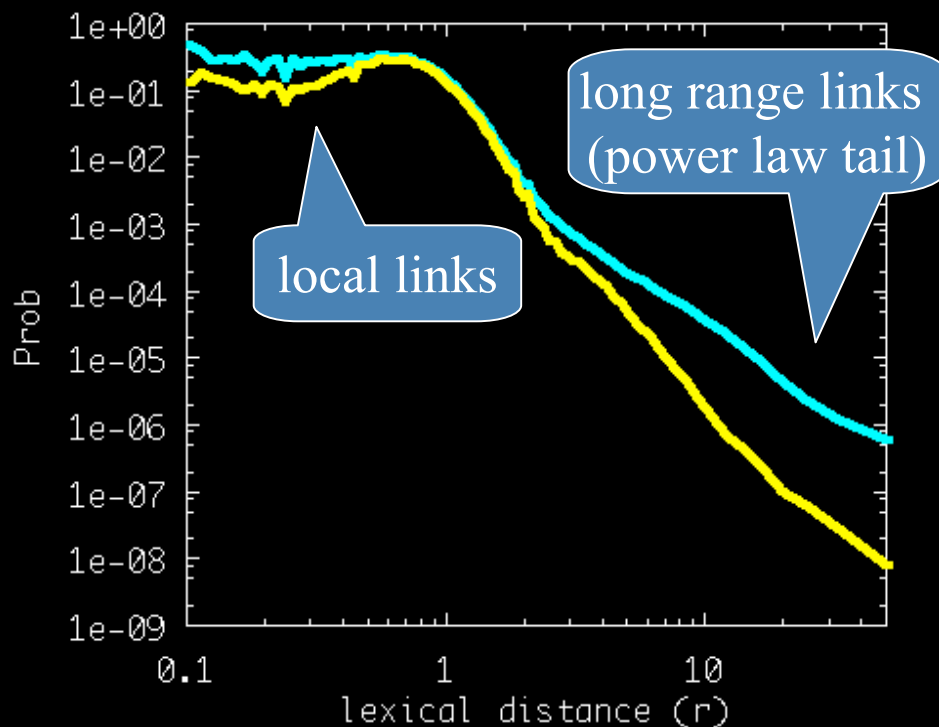


# Is the Web one of these exceptions?

## Geographical model

- Replace lattice distance by lexical distance

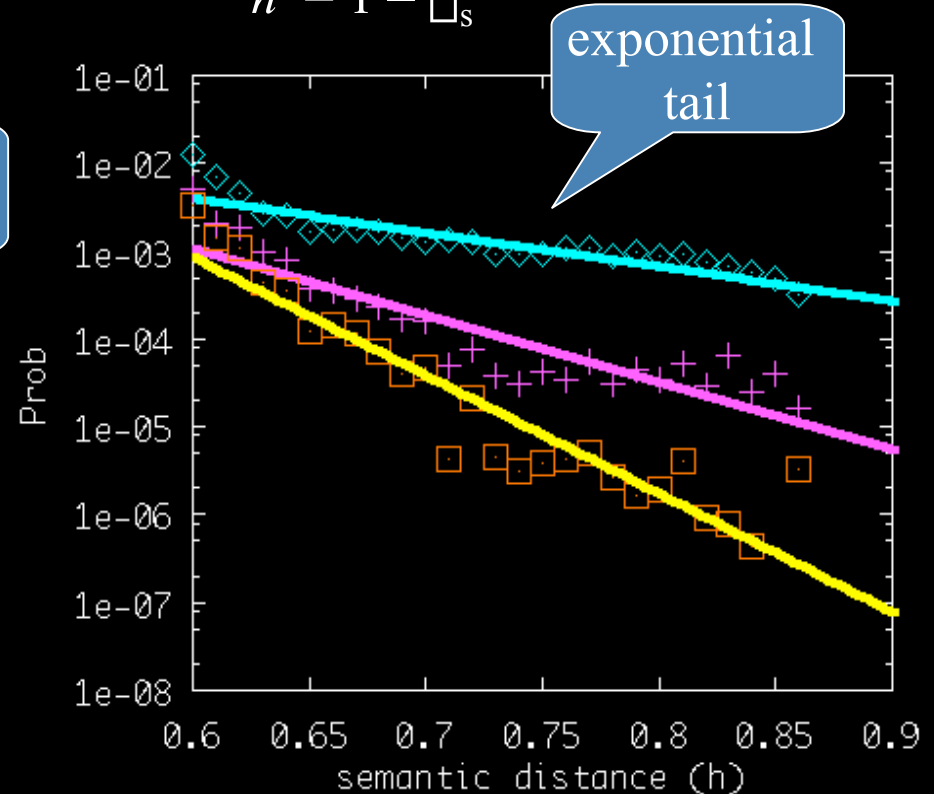
$$r = (1 / \square_c) - 1$$



## Hierarchical model

- Replace tree distance by semantic distance

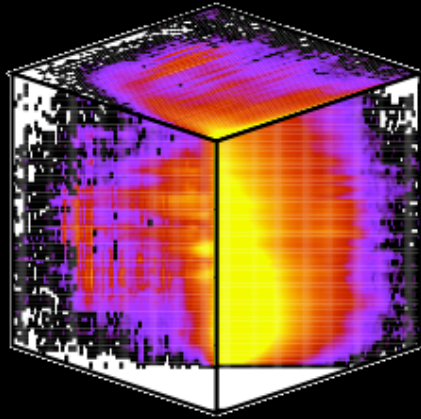
$$h = 1 - \square_s$$





# Talk outline

- The topologies of the Web
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- Semantic maps



# Semantic maps: define “local” Precision and Recall

$$P(s_c, s_l) = \frac{\sum_{\{p, q: \square_c = s_c, \square_l = s_l\}} \square_s(p, q)}{|\{p, q: \square_c = s_c, \square_l = s_l\}|}$$

Averaging  
semantic  
similarity

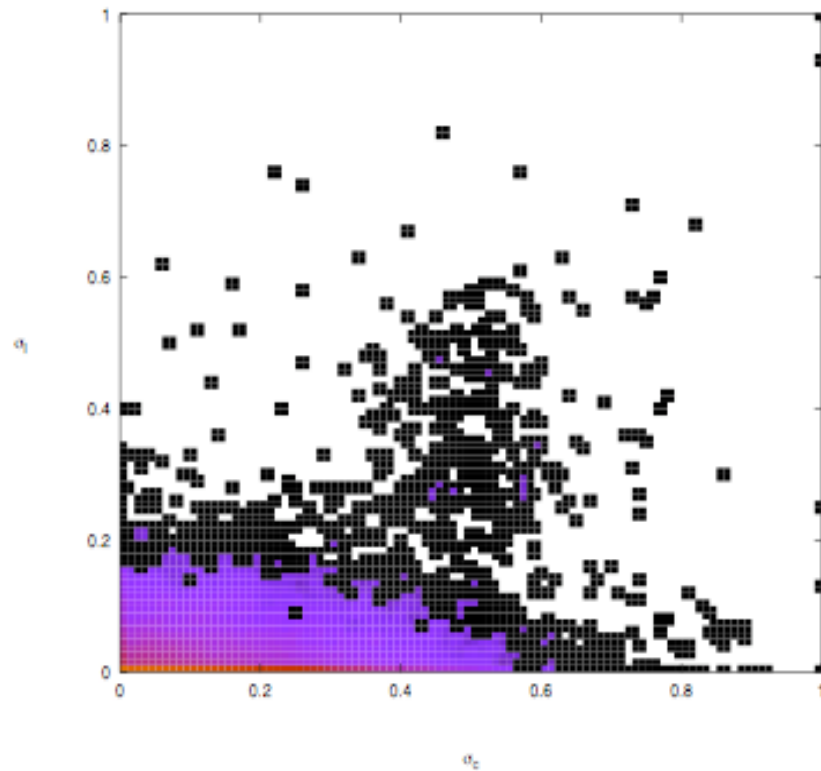
$$R(s_c, s_l) = \frac{\sum_{\{p, q: \square_c = s_c, \square_l = s_l\}} \square_s(p, q)}{\sum_{\{p, q\}} \square_s(p, q)}$$

Summing  
semantic  
similarity

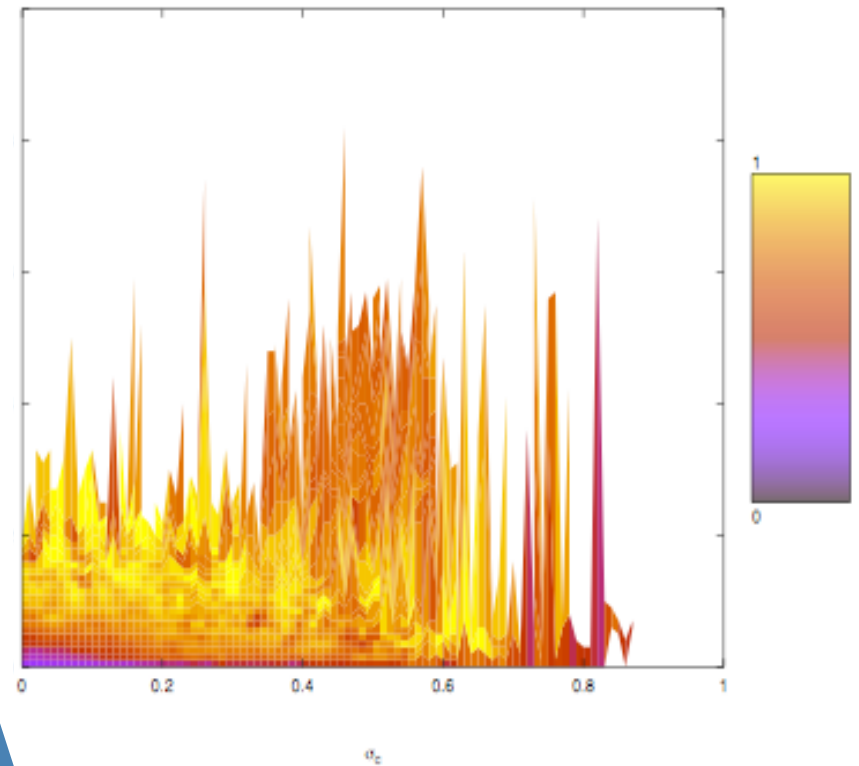


# Semantic maps: *Business*

log Recall



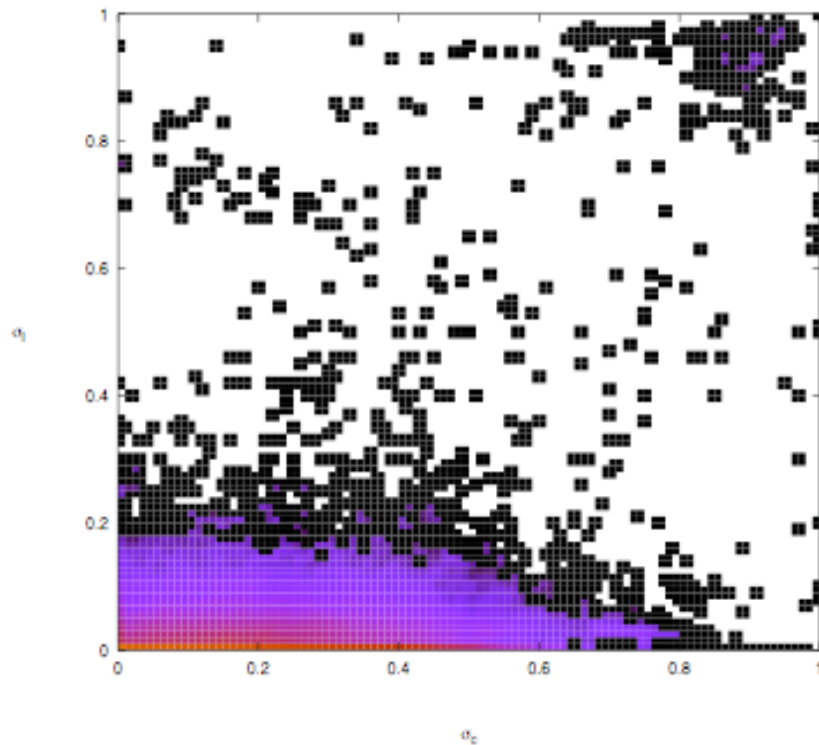
Precision



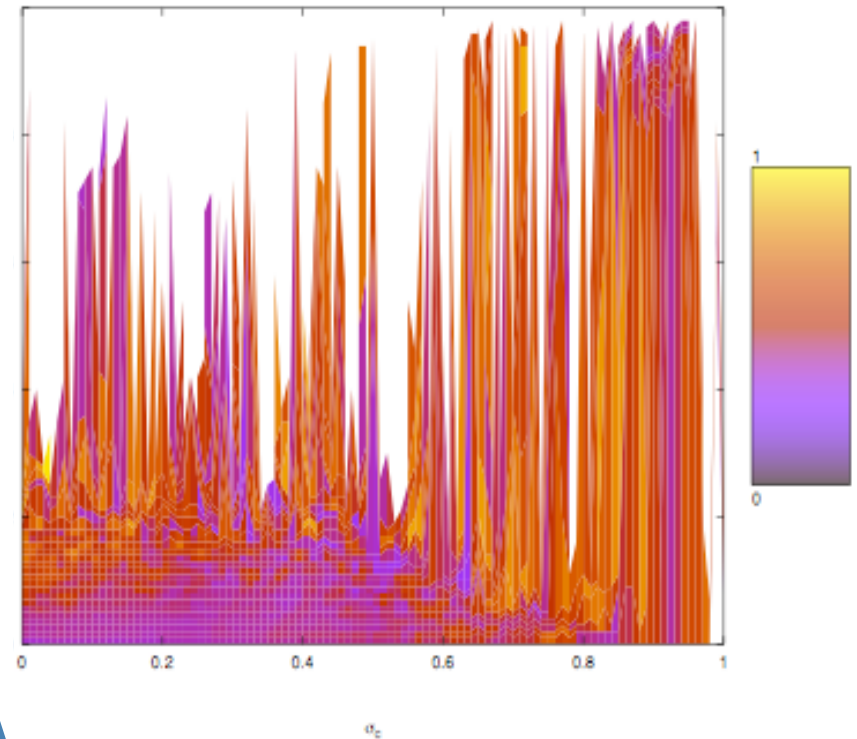


# Semantic maps: *Adult*

log Recall



Precision





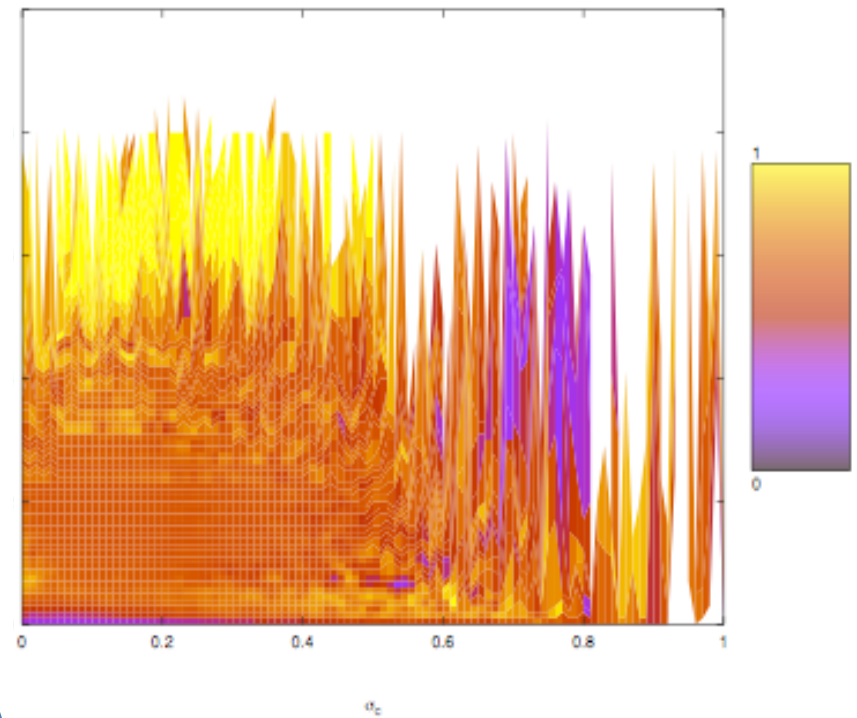
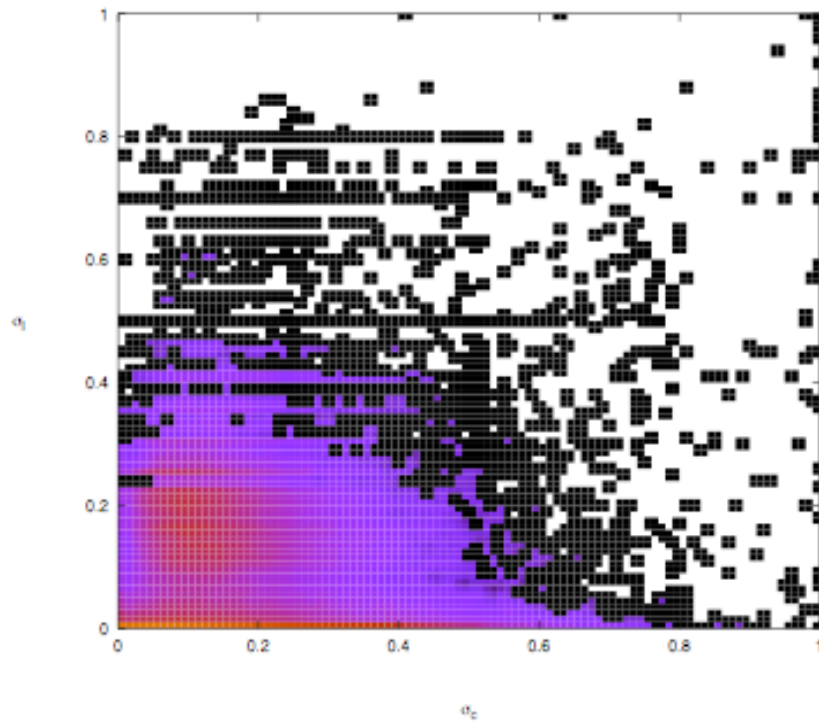


# Semantic maps: *Computers*

log Recall



Precision

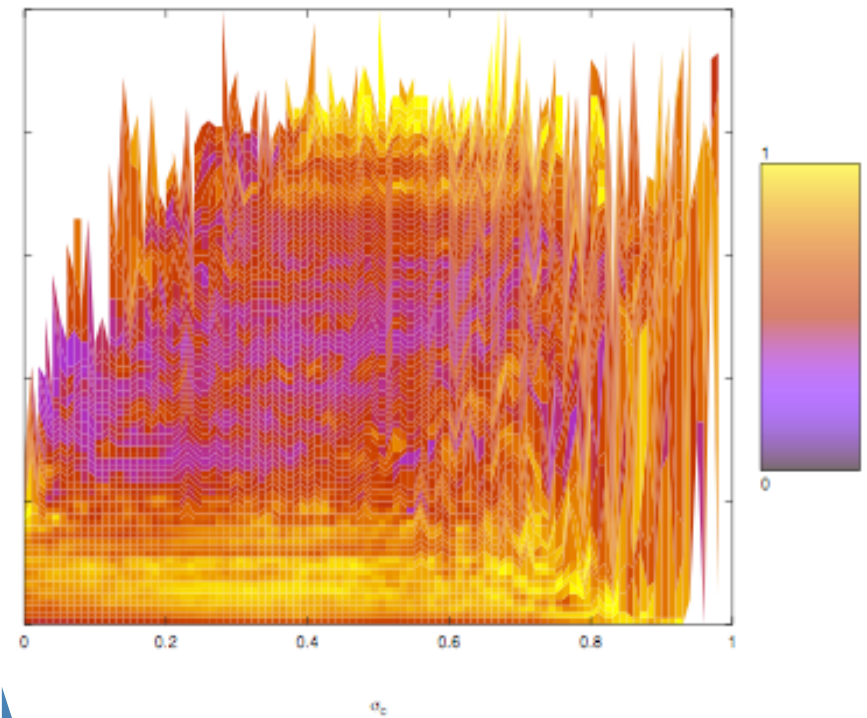
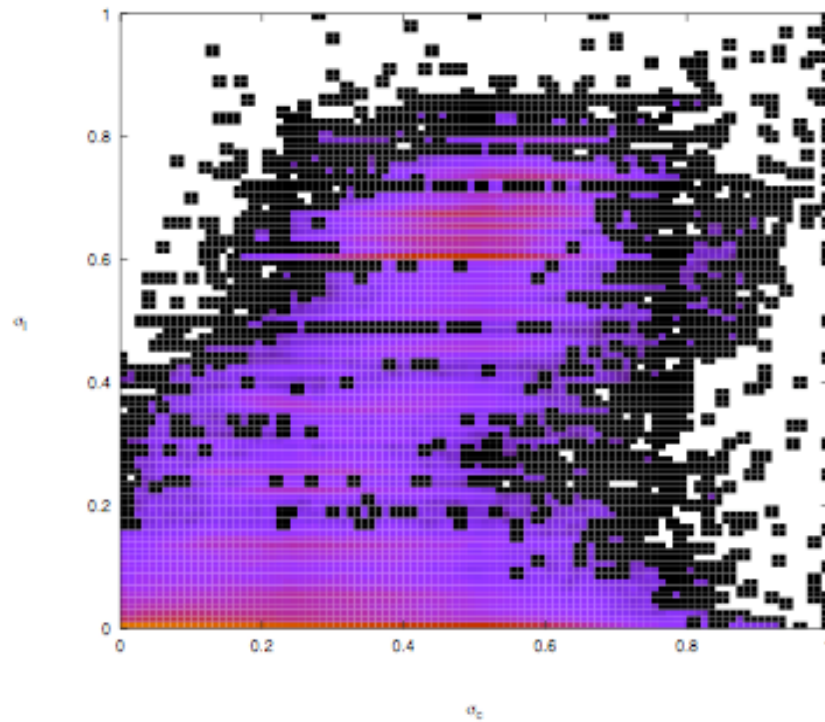




# Semantic maps: *Home*

log Recall

Precision

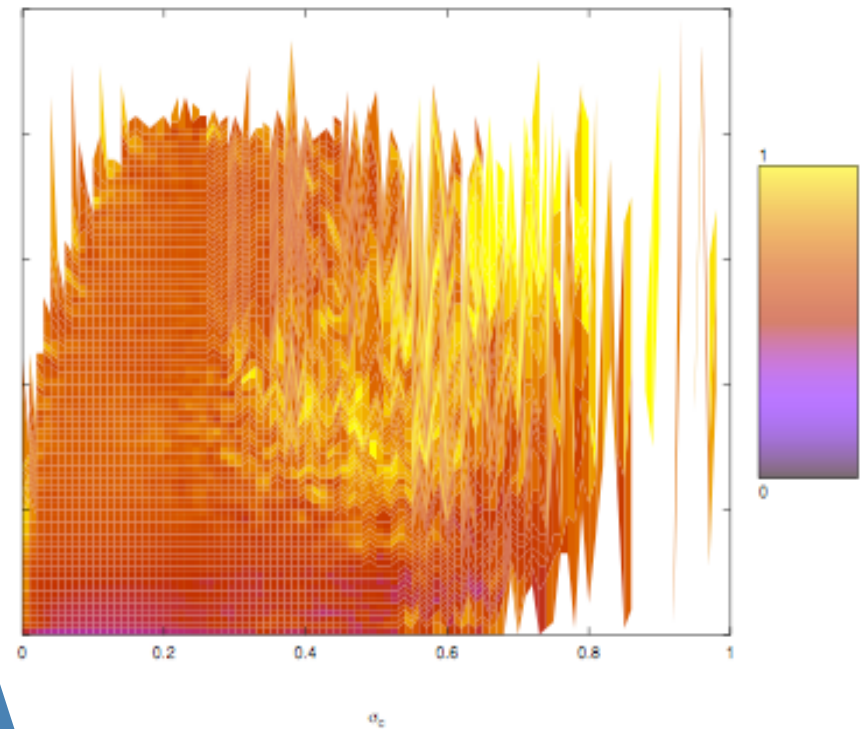
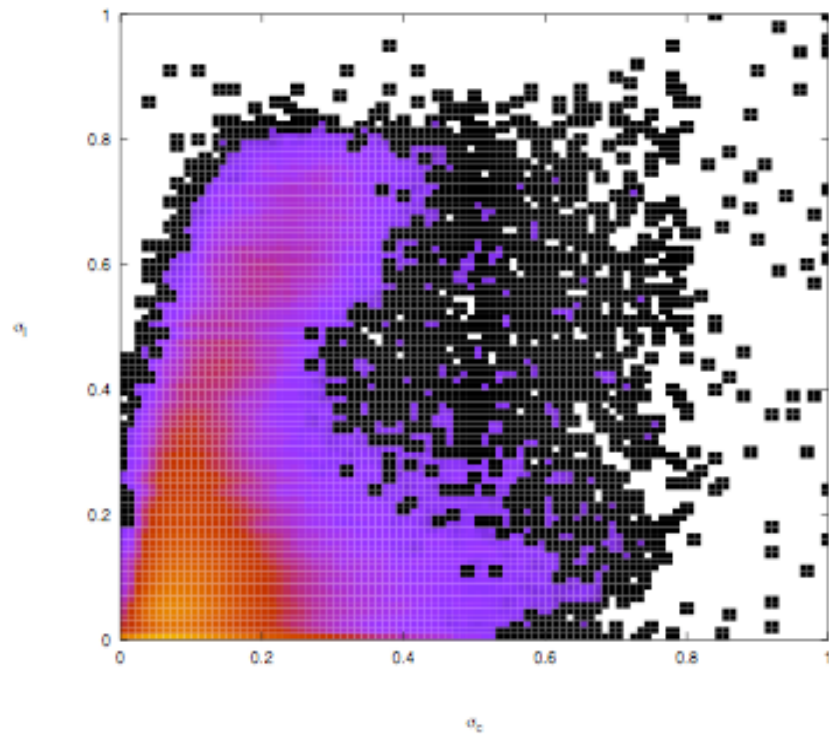




# Semantic maps: *News*

log Recall

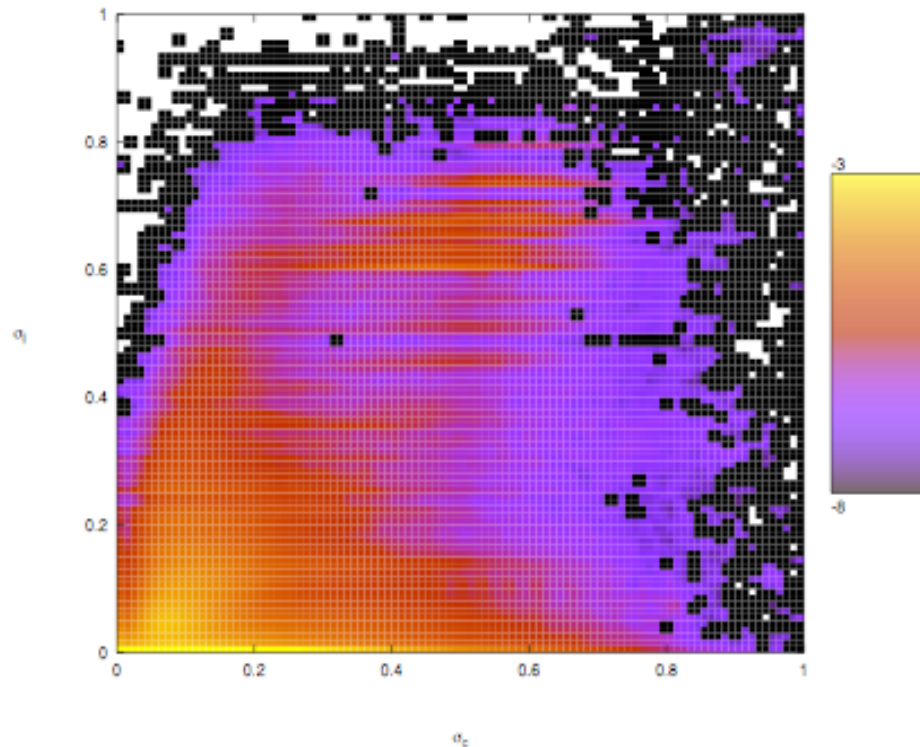
Precision



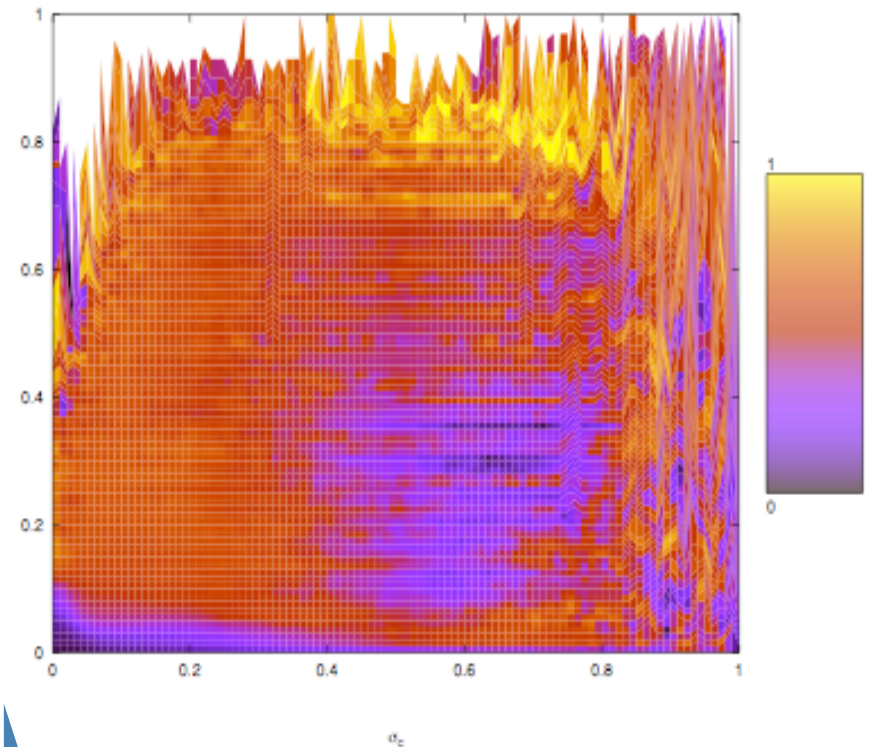


# Semantic maps: all pairs

log Recall



Precision





# So what?

- Interpret performance of search engines
- Understand “ranking optimization”
  - vs filtering
  - vs combinations
- Topical signatures for topical/community portals
- Design “better” (and more scalable) crawlers
  - Topic driven
  - Query driven
  - User/community/peer driven
- Competitive intelligence, security applications





# Talk outline

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- Semantic maps
- Questions?

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Research supported by NSF  
CAREER Award IIS-0133124